



Vector



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TOP Maths IGCSE



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Column vector

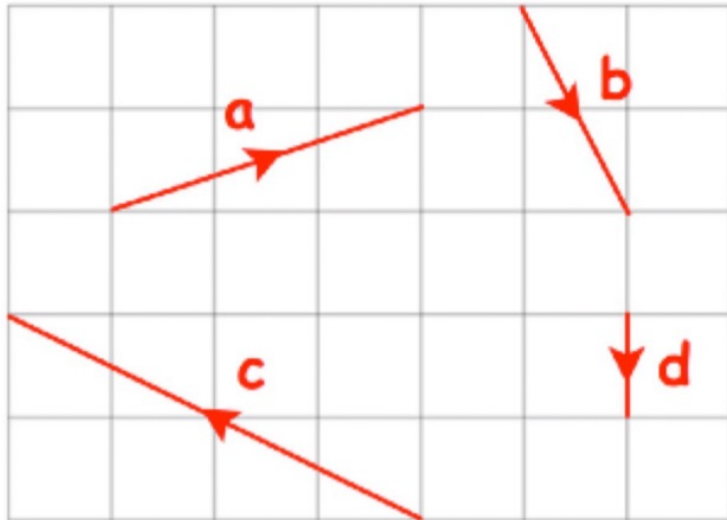
On a grid, draw and label the following vectors.

(a) $\mathbf{a} = \begin{pmatrix} 5 \\ 2 \end{pmatrix}$ (b) $\mathbf{b} = \begin{pmatrix} -1 \\ 3 \end{pmatrix}$ (c) $\mathbf{c} = \begin{pmatrix} -3 \\ -7 \end{pmatrix}$ (d) $\mathbf{d} = \begin{pmatrix} 0 \\ -6 \end{pmatrix}$

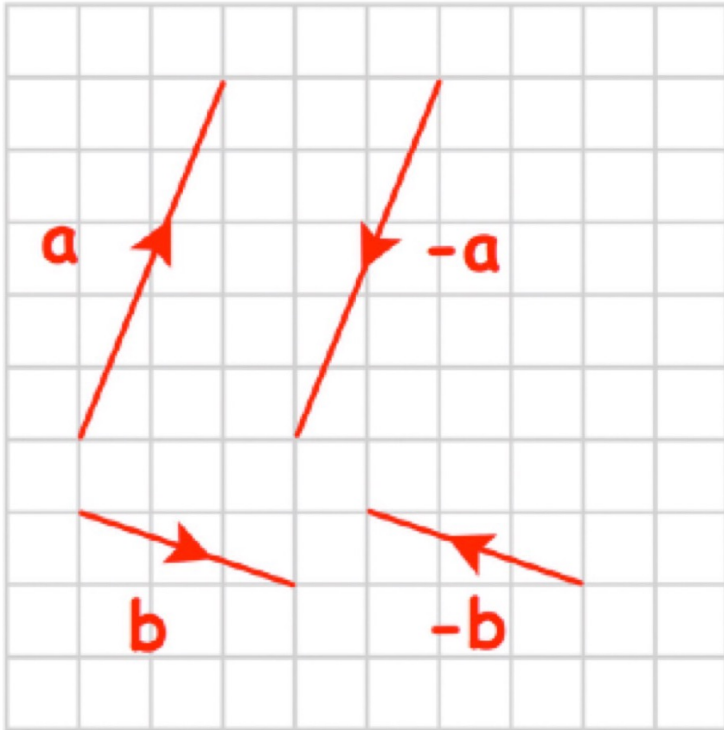
(e) $\mathbf{e} = \begin{pmatrix} 8 \\ -1 \end{pmatrix}$ (f) $\mathbf{f} = \begin{pmatrix} -4 \\ 0 \end{pmatrix}$



The vectors **a**, **b**, **c** and **d** are shown on the grid.



- (a) Write **a** as a column vector
- (b) Write **b** as a column vector
- (c) Write **c** as a column vector
- (d) Write **d** as a column vector



- (a) Write **a** as a column vector
- (b) Write **-a** as a column vector
- (c) Write **b** as a column vector
- (d) Write **-b** as a column vector

Multiplying vector with scalar

$$\text{Given } \mathbf{a} = \begin{pmatrix} 6 \\ 4 \end{pmatrix} \quad \mathbf{b} = \begin{pmatrix} 3 \\ -2 \end{pmatrix} \quad \text{and} \quad \mathbf{c} = \begin{pmatrix} -9 \\ -7 \end{pmatrix}$$

Write the following as column vectors

(a) $3\mathbf{a}$ (b) $2\mathbf{b}$ (c) $5\mathbf{c}$ (d) $\frac{1}{2}\mathbf{a}$ (e) $\frac{1}{4}\mathbf{b}$

$$\text{Given } \mathbf{a} = \begin{pmatrix} 2 \\ 11 \end{pmatrix} \quad \mathbf{b} = \begin{pmatrix} -8 \\ 3 \end{pmatrix} \quad \text{and} \quad \mathbf{c} = \begin{pmatrix} -4 \\ -6 \end{pmatrix}$$

Write the following as column vectors

(a) $-\mathbf{a}$ (b) $-\mathbf{b}$ (c) $-\mathbf{c}$ (d) $-2\mathbf{a}$ (e) $-4\mathbf{b}$ (f) $-\frac{1}{2}\mathbf{b}$

Adding or subtracting vectors

nose to tail RULE

$$\mathbf{a} = \begin{pmatrix} 5 \\ 2 \end{pmatrix} \quad \mathbf{b} = \begin{pmatrix} -1 \\ 3 \end{pmatrix}$$



Adding or subtracting vectors

nose to tail RULE

$$\mathbf{a} = \begin{pmatrix} 5 \\ 2 \end{pmatrix} \quad \mathbf{b} = \begin{pmatrix} -1 \\ 3 \end{pmatrix}$$



Tip 

 For adding and subtracting column vectors

Given $\mathbf{a} = \begin{pmatrix} 3 \\ 0 \end{pmatrix}$ $\mathbf{b} = \begin{pmatrix} 2 \\ 7 \end{pmatrix}$ $\mathbf{c} = \begin{pmatrix} 1 \\ 4 \end{pmatrix}$ $\mathbf{d} = \begin{pmatrix} -4 \\ 3 \end{pmatrix}$ and $\mathbf{e} = \begin{pmatrix} -1 \\ -2 \end{pmatrix}$

(a) $\mathbf{a} + \mathbf{b}$

(b) $\mathbf{b} + \mathbf{c}$

(c) $\mathbf{a} + \mathbf{c}$

(d) $\mathbf{c} + \mathbf{d}$

Given $\mathbf{a} = \begin{pmatrix} 3 \\ 0 \end{pmatrix}$ $\mathbf{b} = \begin{pmatrix} 2 \\ 7 \end{pmatrix}$ $\mathbf{c} = \begin{pmatrix} 1 \\ 4 \end{pmatrix}$ $\mathbf{d} = \begin{pmatrix} -4 \\ 3 \end{pmatrix}$ and $\mathbf{e} = \begin{pmatrix} -1 \\ -2 \end{pmatrix}$

(e) $\mathbf{a} - \mathbf{d}$

(f) $\mathbf{e} - \mathbf{b}$

(g) $\mathbf{e} - \mathbf{d}$

(h) $3\mathbf{a} - \mathbf{b}$

Equivalent vectors

Two vectors are equivalent if they have the same direction and length.

Parallel vectors

True or false ?

$$\begin{pmatrix} 3 \\ 1 \end{pmatrix} \text{ is parallel to } \begin{pmatrix} 9 \\ 3 \end{pmatrix}$$

$$\begin{pmatrix} 2 \\ 0 \end{pmatrix} \text{ is parallel to } \begin{pmatrix} 4 \\ 0 \end{pmatrix}$$

$$\begin{pmatrix} -1 \\ 1 \end{pmatrix} \text{ is parallel to } \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

Position vector and coordinate

Example 1

Point P is the coordinate (5,8)

Find position vector of P

Example 2

Position vector of M is $\begin{pmatrix} 5 \\ -3 \end{pmatrix}$

Find the coordinate of point M

Example 3

P is the point (5, 6). $\overrightarrow{PQ} = \begin{pmatrix} 3 \\ 1 \end{pmatrix}$

Find the co-ordinates of Q.

Example 4

If D has coordinates $(6, 2)$ and E has coordinates $(0, 5)$, find the column vector for \overrightarrow{DE} .

Example 5

Find the column vector \overrightarrow{XY} where X and Y have coordinates (3, 1) and (2, -5) respectively.

Magnitude or modulus of vector

Find magnitude for each vector

$$\mathbf{a} = \begin{pmatrix} 3 \\ 4 \end{pmatrix}$$

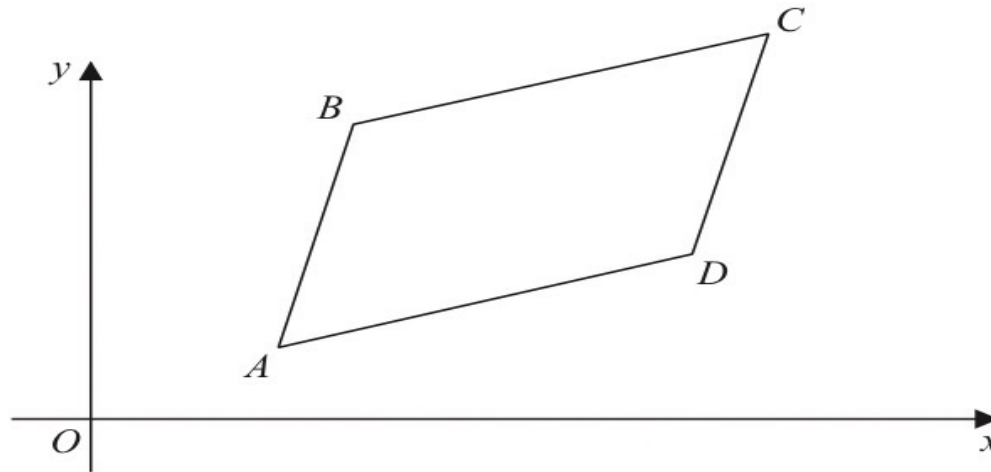
$$\mathbf{b} = \begin{pmatrix} 4 \\ 1 \end{pmatrix}$$

$$\mathbf{c} = \begin{pmatrix} 5 \\ 12 \end{pmatrix}$$

$$\mathbf{d} = \begin{pmatrix} -3 \\ 0 \end{pmatrix}$$

Exam Style Questions

The diagram shows parallelogram $ABCD$.



$$\vec{AB} = \begin{pmatrix} 1 \\ 3 \end{pmatrix} \quad \vec{AC} = \begin{pmatrix} 12 \\ 15 \end{pmatrix}$$

The point B has coordinates $(6, 8)$

Work out the coordinates of the point C .

Exam Style Questions

$ABCD$ is a trapezium.

$$\vec{DC} = 3\vec{AB}$$

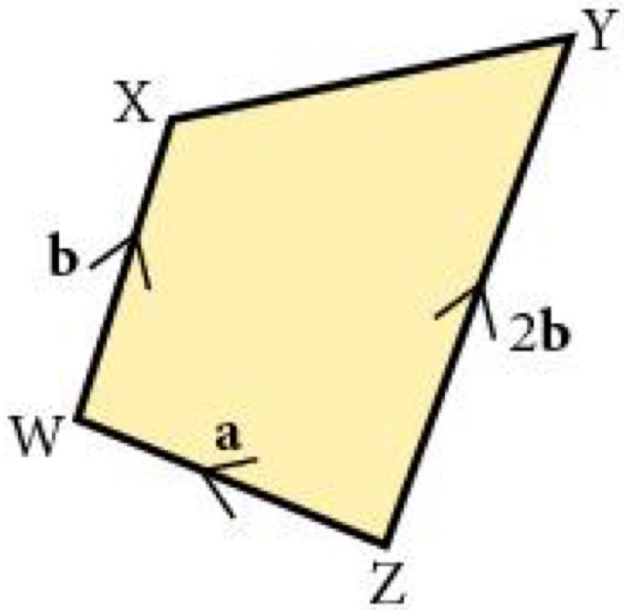
$$\vec{DA} = \begin{pmatrix} -1 \\ 2 \end{pmatrix} \quad \vec{DB} = \begin{pmatrix} -3 \\ 5 \end{pmatrix}$$

Find the exact magnitude of \vec{BC}



Vector Geometry

Q1.



Find in term of a and b

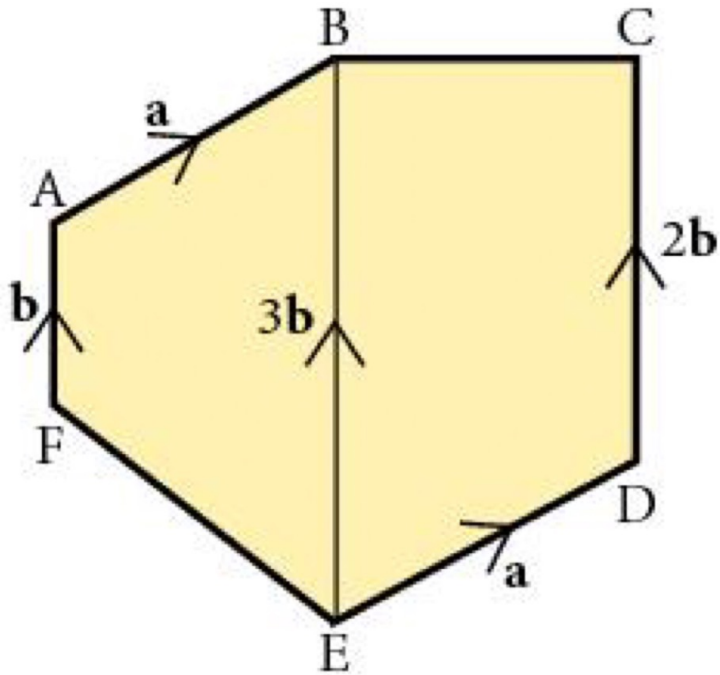
1. \vec{XW}

2. \vec{XZ}

3. \vec{XY}

Q2.

Find in term of a and b

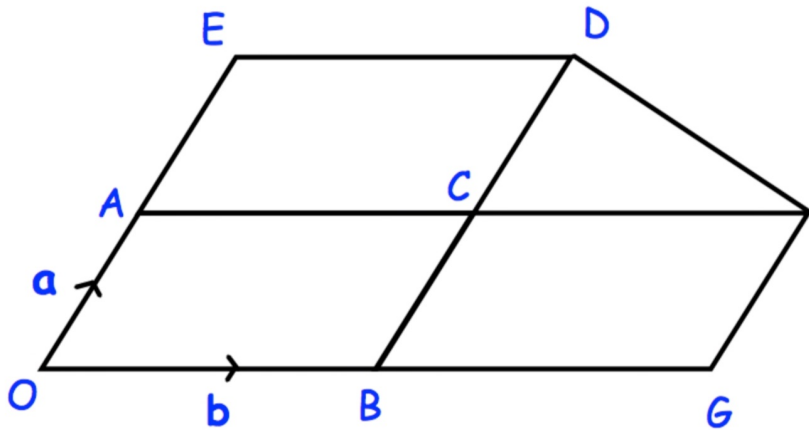


1. \overrightarrow{BF}

2. \overrightarrow{FE}

3. \overrightarrow{AD}

Q3. In diagram OBDE and OAFG are parallelogram
 B is the midpoint of OG And A is the midpoint of OE



Find in term of a and b

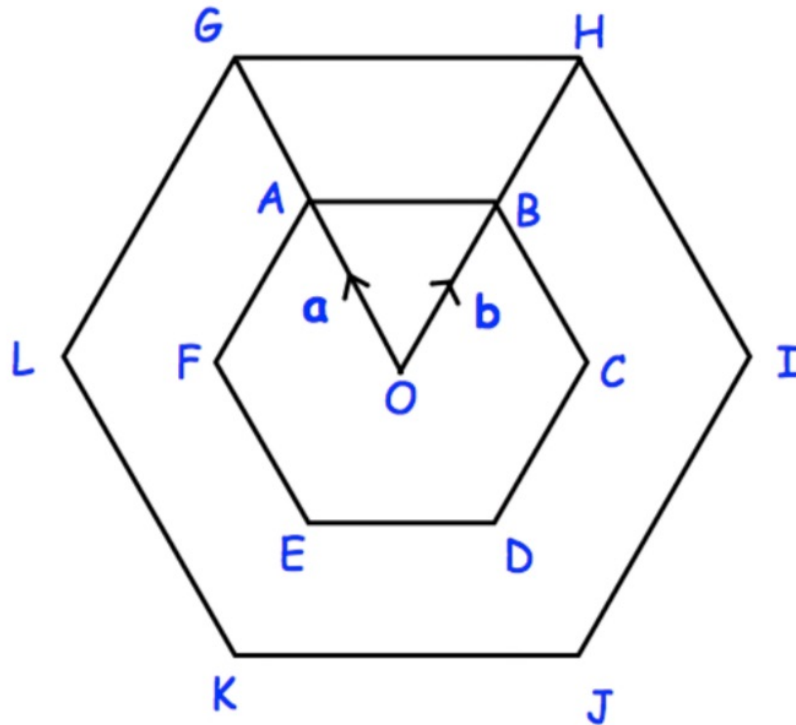
1. \vec{OC}

2. \vec{BA}

3. \vec{DF}

4. Show that \vec{EG} and \vec{DF} are parallel

Q4.



ABCDEF and GHIJKL are regular hexagons with centre O.
GHIJKL is an enlargement of ABCDEF, with scale factor 2.

Find in term of a and b

1. \vec{AB}

2. \vec{OG}

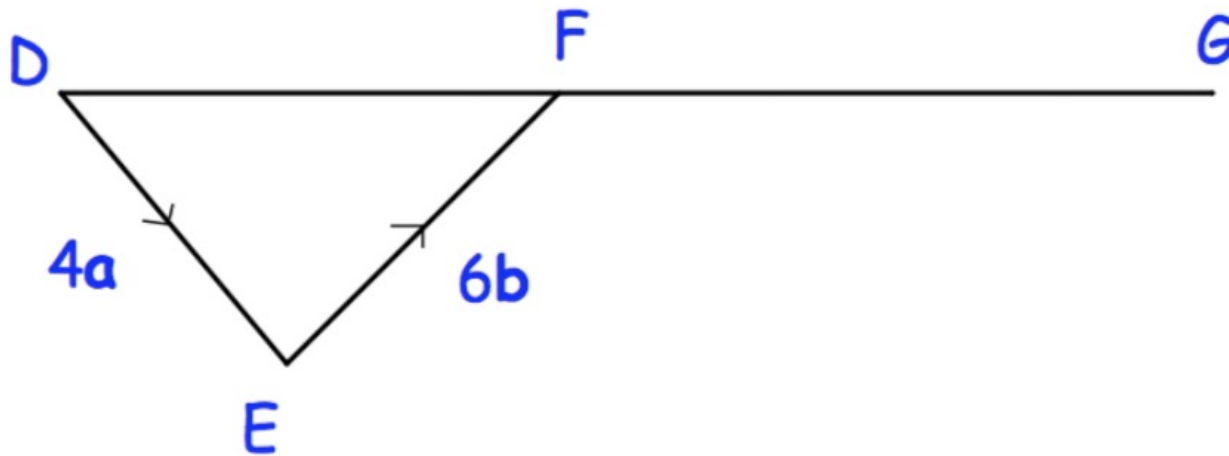
3. \vec{OE}

4. \vec{FC}

5. \vec{IK}

Q5. DFG is a straight line.

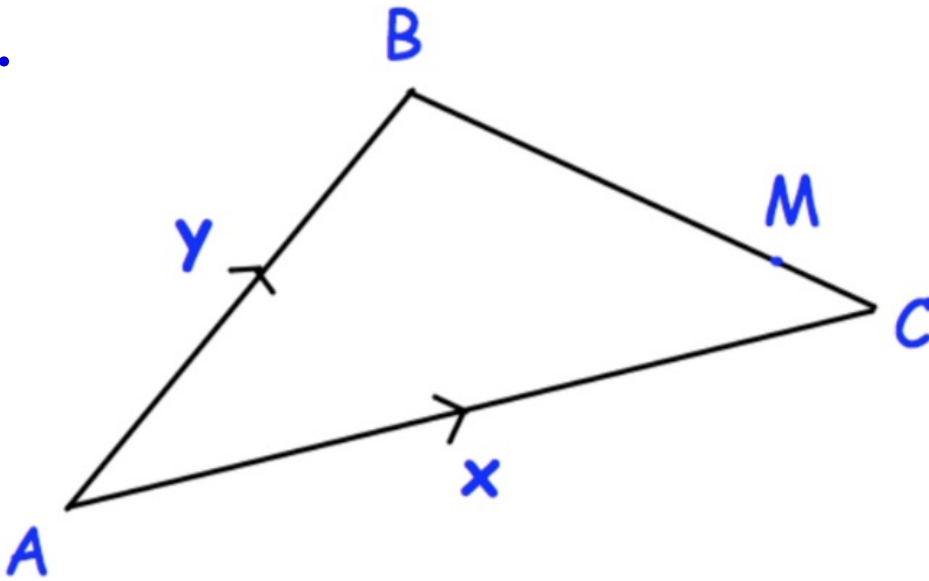
$$\vec{DE} = 4\mathbf{a} \quad \text{and} \quad \vec{EF} = 6\mathbf{b}$$



1. Find \vec{DF} in term of \mathbf{a} and \mathbf{b}

2. Given that $\vec{DF} : \vec{FG} = 2 : 3$, Find \vec{DG}

Q6.



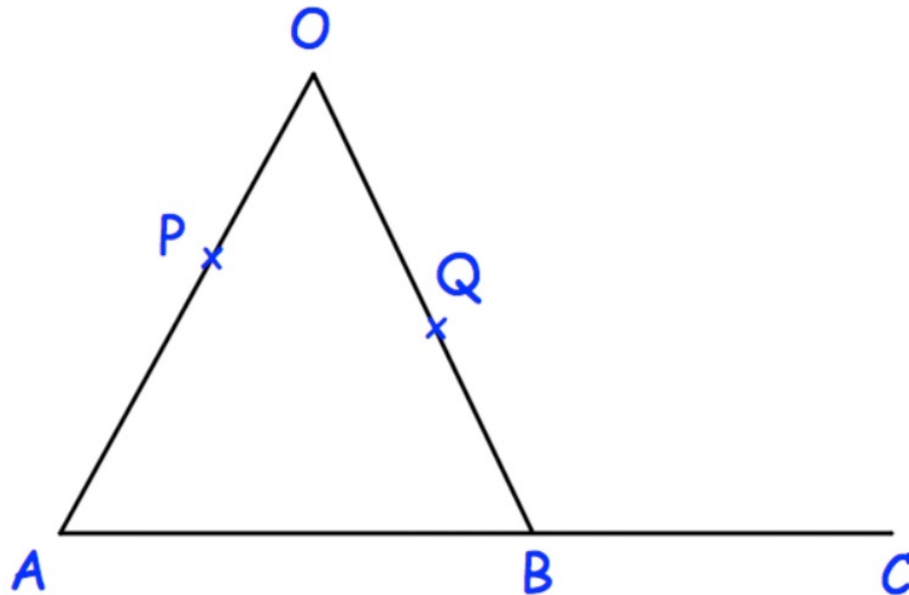
ABC is a triangle, M lies on BC such that $BM = \frac{5}{6} BC$

Find in term of x and y

1. \vec{BC}
2. \vec{BM}
3. \vec{AM}

How to show 3 points lie on the same straight line

Q7.



AOB is a triangle.
P is a point on AO.

$$\vec{AB} = 2\mathbf{a}$$

$$\vec{AO} = 6\mathbf{b}$$

$$AP:PO = 2:1$$

Find in term of \mathbf{a} and \mathbf{b}

1. \vec{OB}

2. Q is the midpoint of OB and B is the midpoint of AC
Show that PQC is a straight line

- Q8. OAB is a triangle. $OA = 4a$ and $OB = 2b$. M is the mid point of AB .
 P is the point on OB such that $OP : PB = 2 : 1$
 Q is the point on AP such that OQM is a straight line.

Find the ratio of $OQ : QM$

