

DENARY ARITHMETIC

Decimal	0	1	2	3	4	5	6	7	8	9
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❖ $5 + 1 = ?$

❖ $5 + 3 = ?$

❖ $9 + 1 = ?$

DENARY ARITHMETIC

❖ Place value table

❖ 5

❖ 26

❖ 189

❖ $9 + 1 = 10$

❖ $18 + 2 = 20$

❖ $19 + 3 = 22$

Place value table			
10^3	10^2	10^1	10^0
1000	100	10	1

DENARY ARITHMETIC

Worked example				
369 + 733				
Place values	10^3	10^2	10^1	10^0
	1000	100	10	1
Carry over	1	1	1	
		3	6	9
		7	3	3
Total	1	1	0	2
		100 + 300 + 700 = 1100 The 1000 is carried over leaving 100.	10 + 60 + 30 = 100 The 100 is carried over.	9 + 3 = 12 The 10 is carried over leaving 2.

Binary addition works in the same way but a 'carry over' is needed if the result is greater than 1.

CONVERTING DECIMAL TO BINARY (BASE10 - BASE2)

❖ 70 in decimal to binary

❖ Follow these steps

1. Write place value table
2. Multiple each place value with 0 or 1;
Put 1 into the place values that can
make to total of result equals to the
target

2^7	2^6	2^5	2^4	2^3	2^2	2^1	2^0
128	64	32	16	8	4	2	1

CONVERTING DECIMAL TO BINARY (BASE10 - BASE2)

❖ Convert these denary numbers to binary

❖ 3

❖ 8

❖ 13

❖ 100

❖ 255

CONVERTING BINARY TO DECIMAL (BASE2 – BASE10)

❖ 01000110 in binary to decimal

❖ Follow these steps

1. Write place value table
2. Put binary into the place value table
3. Multiply each place value with 0 or 1
4. Sum up the value

2^7	2^6	2^5	2^4	2^3	2^2	2^1	2^0
128	64	32	16	8	4	2	1

CONVERTING BINARY TO DECIMAL (BASE2 – BASE10)

❖ Convert these binary numbers to denary

❖ 10

❖ 101

❖ 0110

❖ 1010

❖ 10110

Binary	0	1
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CONVERTING BINARY TO DECIMAL (BASE2 – BASE10)

- ❖ Convert these binary numbers to denary
- ❖ Highest value of 4-bit binary
- ❖ Lowest value of 4-bit binary

BINARY ARITHMETIC

❖ Add up these numbers

❖ $0+0 = ?$

❖ $0+1 = ?$

❖ $1+0 = ?$

❖ $1+1 = ?$

❖ $1+1+1 = ?$

BINARY ARITHMETIC

Worked example								
11010110 + 01100111								
Place values	2^7	2^6	2^5	2^4	2^3	2^2	2^1	2^0
	128	64	32	16	8	4	2	1
Carry over	1				1	1		
1	1	1	0	1	0	1	1	0
	0	1	1	0	0	1	1	1
Total	0	0	1	1	1	1	0	1
	128 + 128 = 256 This should be carried over.	64 + 64 = 128 The 128 is carried over.	No carry over needed.	No carry over needed.	No carry over needed.	4 + 4 + 4 = 12 The 8 is carried over leaving one 4.	2 + 2 = 4 The 4 is carried over.	No carry over needed.

OVERFLOW

- What happens when $70 + 226$
 - $70 + 226 = 296$
 - The highest value of eight bits binary is 255
 - Thus, 296 cannot be represented in eight bits binary
 - The computer reports an error as “overflow”
 - When the result is too big to be represented by the given number of bits

$$\begin{array}{r} 1 11 \\ 01000110_{(2)} \\ + 11100010_{(2)} \\ \hline 100101000_{(2)} \end{array}$$