

BINARY, SIGNED AND UNSIGNED NUMBER

❖ What about negative numbers in binary?

❖ There are 2 methods for representing a negative number

1. Sign and magnitude

❖ Reserve the most significant bit(MSB) for sign

❖ 0 for positive and 1 for negative

❖ $(0101)_2 = (5)_{10}$

❖ $(1101)_2 = (-5)_{10}$

Signed denary number to be represented	Sign and magnitude representation	Two's complement representation
+7	0111	0111
+6	0110	0110
+5	0101	0101
+4	0100	0100
+3	0011	0011
+2	0010	0010
+1	0001	0001
+0	0000	0000
-0	1000	Not represented
-1	1001	1111
-2	1010	1110
-3	1011	1101
-4	1100	1100
-5	1101	1011
-6	1110	1010
-7	1111	1001
-8	Not represented	1000

SIGN AND MAGNITUDE SYSTEM

- Write these number in binary with sign and magnitude system
- 4-bit
 - 10
 - -5
- 8-bit
 - 65
 - -20

BINARY, TWO'S COMPLEMENT

2. Two's complement

❖ There are 2 methods to convert normal binary to Two's complement

❖ Method 1

1. One's complement

❖ Invert each bit; $0 \Rightarrow 1$ and $1 \Rightarrow 0$

2. Two's complement

❖ Add 1 to the least significant digit (LSD)

Example, convert 5 to -5 by using two's complement

BINARY, TWO'S COMPLEMENT

- ❖ Convert these number to negative value using 1st method

- ❖ 4-bit

- ❖ 10

- ❖ 6

- ❖ 8-bit

- ❖ 20

- ❖ 10

- ❖ Extra question

- ❖ What would happen if we use two's complement with -20

BINARY, TWO'S COMPLEMENT

❖ Two's complement

❖ Method 2

1. Consider the most significant digit is negative
2. Multiple each place value with 0 or 1; Put 1 into the place values that can make to total of result equals to the target

Example, covert 5 to -5 by using two's complement

-128	64	32	16	8	4	2	1

BINARY, TWO'S COMPLEMENT

❖ Convert these number to negative value using 2nd method

❖ 4-bit

❖ 10

❖ 6

❖ 8-bit

❖ 20

❖ 10

BINARY TWO'S COMPLEMENT

- Subtraction?
 - Computer processors don't have a circuit for subtraction
 - $28 - 5$: computers cannot do the calculation
 - $28 + (-5)$: computers can do the calculation
 - Use of two's complement

Worked example

Add 28 and -5 .

This is more difficult. The result should be 23.

The two's complement representation of -5 is

5	0	0	0	0	0	1	0	1
Flip	1	1	1	1	1	0	1	0
Add 1	1	1	1	1	1	0	1	1

Adding binary 28 to binary -5 gives

0	0	0	1	1	1	0	0
1	1	1	1	1	0	1	1
0	0	0	1	0	1	1	1

The result is 00010111, which is the binary equivalent of 23.

BINARY TWO'S COMPLEMENT

❖ Show working for $-5 + 10$, using 4-bit binary